

The roles of equatorial trapped waves and internal inertia-gravity waves in driving the QBO

Yoshio Kawatan¹, Kaoru Sato², Timothy J. Dunkerton³
Shingo Watanabe¹, Saburo Miyahara⁴, Masaaki Takahashi⁵

1. JAMSTEC, 2. Univ. Tokyo, 3. NWRA, 4. Kyushu Univ., 5. CCSR, Univ. Tokyo



Kawatani, Y., K. Sato, T. J. Dunkerton, S. Watanabe, S. Miyahara, and M. Takahashi, 2010
The roles of equatorial trapped waves and internal inertia-gravity waves in driving
the quasi-biennial oscillation.

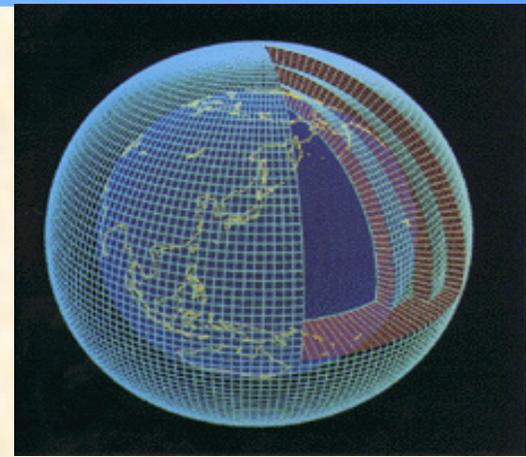
Part I: Zonal mean wave forcing, J. Atmos. Sci. 67, 963-980

Part II: Three-dimensional distribution of wave forcing, J. Atmos. Sci, 67, 981-997

Model Description

<CCSR/NIES/FRCGC AGCM version 5.7b>

- **T213** ($\Delta\lambda$ and $\Delta\phi \sim 0.56^\circ$ $\Delta H = \sim 60$ km at EQ)
minimum resolvable horizontal wavelengths: ~ 188 km
- **L256 (0-85km)**, Sponge layer above 80km (6-level)
 $\Delta Z = 300$ m from the upper troposphere to the mesosphere
- **GWD parameterization : None, resolved waves only!**
- Cumulus parameterization : Arakawa-Schubert
- Realistic topography and SST/Sea ice
- Sampling time interval: 1-hour
- Simulated period: 3-years

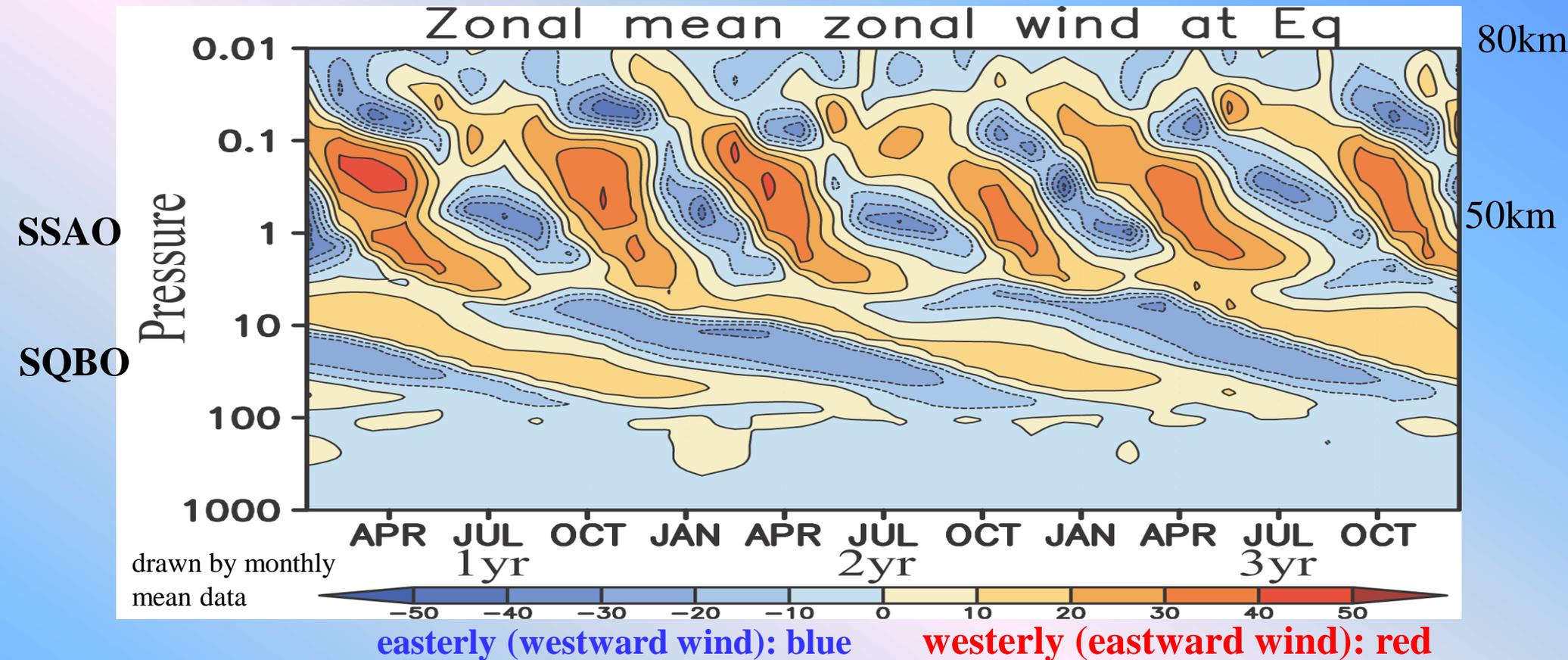


GCM: primitive equation

$$\frac{|w'|}{(u'^2 + v'^2)^{1/2}} \approx (k^2 + l^2)^{1/2} / m \ll 1, \quad \frac{\omega}{N} \approx \frac{(k^2 + l^2)^{1/2}}{m} \ll 1$$

GWs with period much longer than Brunt-Väisälä period

Time-height cross section of zonal mean zonal wind at equator for 3-years

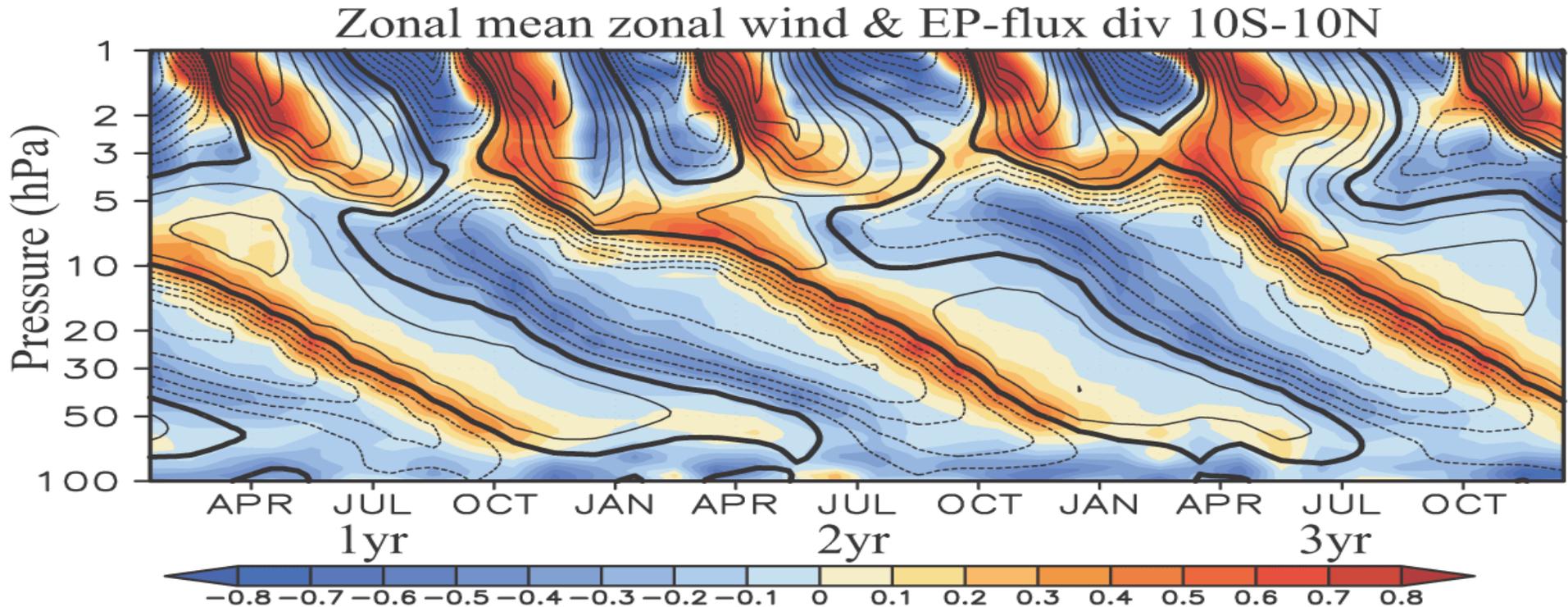


QBO-like oscillations with periods ~ 15 months
easterly (westward wind): ~ -25 (m/s)
westerly (eastward wind): ~ 15 (m/s) at 30hPa
Bottom level: ~ 80 hPa, period: ~ 15 month

SSAO

first cycle $>$ second cycle
westward wind : -70 (m/s)
eastward wind: 35 (m/s)
(when seen in daily data)

Time-height cross section of zonal mean U & EP-flux DIV 10S-10N



Blue: westward forcing

Red: eastward forcing

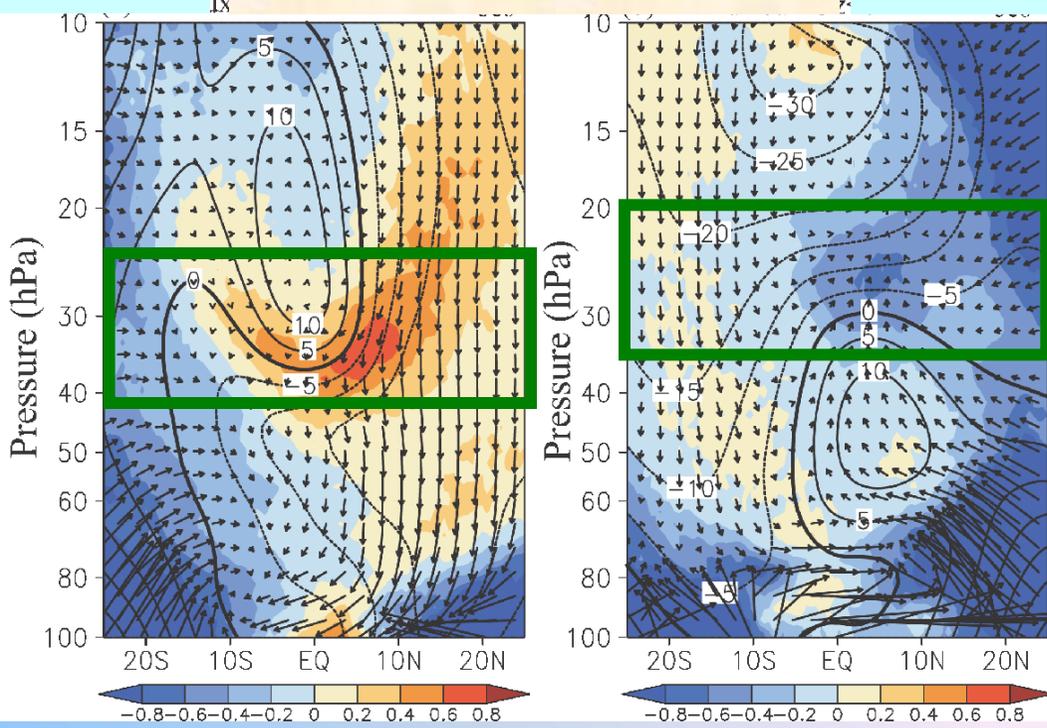
Maximum **eastward forcing** $\sim 0 \text{ ms}^{-1}$ around **eastward wind shear** $U_z > 0$

Maximum **westward forcing** $\sim -10 \text{ ms}^{-1}$ around **westward wind shear** $U_z < 0$

spontaneously generated waves resolved in the model drive the QBO

1. simulated wave forcing might not be much overestimated compared to past studies (validation of wave momentum flux has been conducted)
2. equatorial upwelling w^* might be about half of that in the real atmosphere

Uz>0 Jul EP-flux & its div of all waves Uz<0 Jan



Maximum wave forcing in the shear zone not symmetrically distributed on the equator waves other than EQWs also contribute

eastward wave forcing during Uz>0
 $2 \text{ ms}^{-1} < Cx < 20 \text{ ms}^{-1}, s \leq 140$

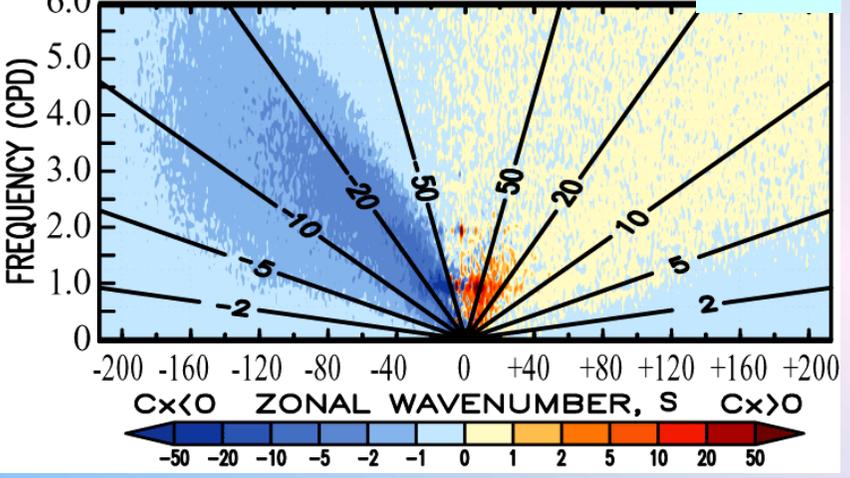
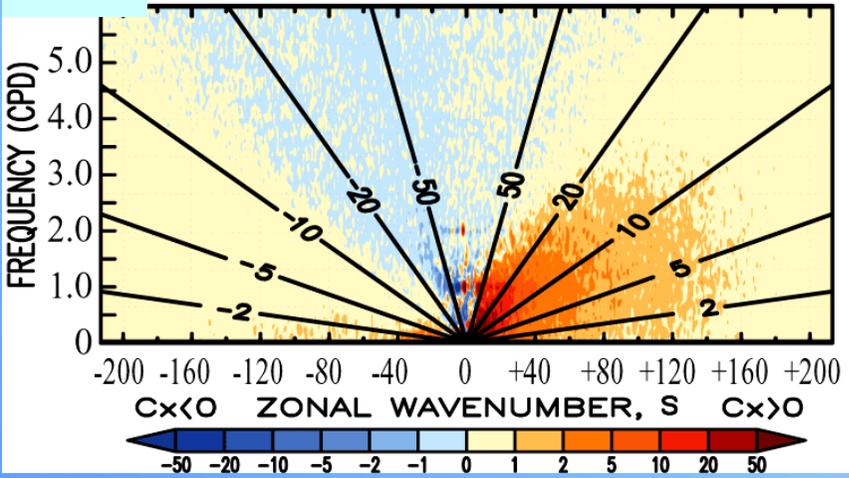
westward wave forcing during Uz<0
 $-30 \text{ m s}^{-1} < Cx < -5 \text{ ms}^{-1}, s \leq 180$

wave forcing with smaller horizontal scale faster Cx dominated in the Uz<0 waves with continuous Cx contribute

zonal wavenumber - frequency distribution of EP-flux divergence (10S-10N)

Uz>0 (c) EP-flux div 45-25hPa Jul Uz>0

(d) EP-flux div 35-20hPa Jan Uz<0



red: eastward forcing

blue: westward forcing

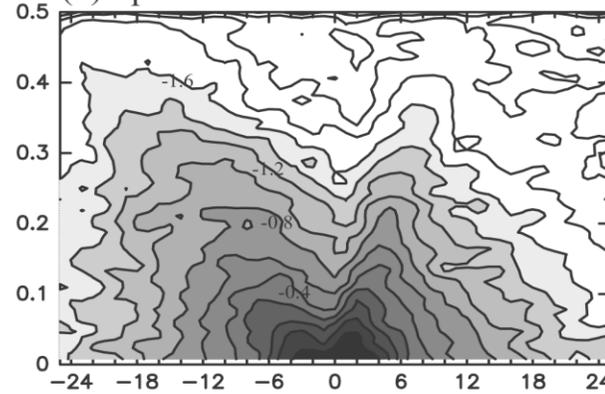
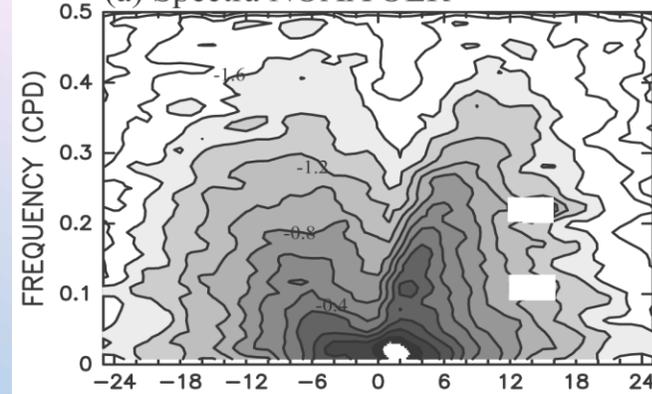
lines: Cx

Obs (NOAA OLR)

T213L256

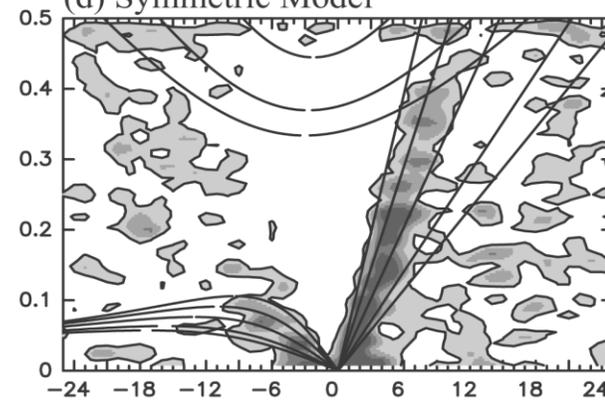
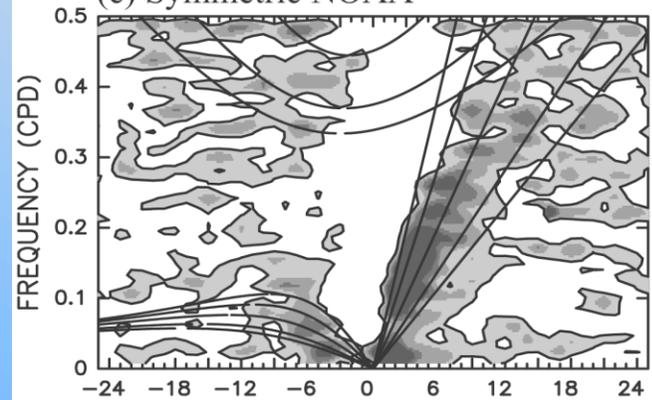
(a) Spectra NOAA OLR

(b) Spectra T213L256



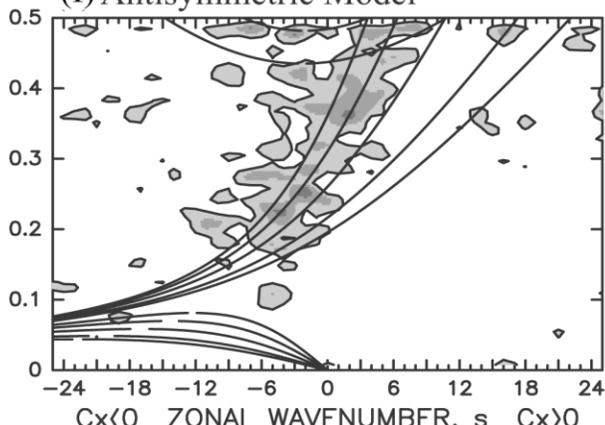
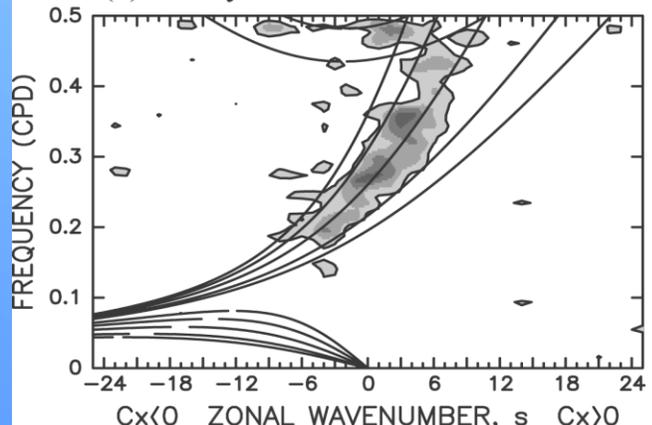
(c) Symmetric NOAA

(d) Symmetric Model



(e) Antisymmetric NOAA

(f) Antisymmetric Model



OLR spectra

zonal wavenumber – frequency
(10S-10N average)

top: $(S+A)/2$

mid: symmetric

bottom: Antisymmetric

he of 8, 12, 25, 50, and 90 m of EQW
Kelvin waves, $n = 1$ ER
MRG waves and $n = 0$ EIGWs

Lin *et al.* (2006)

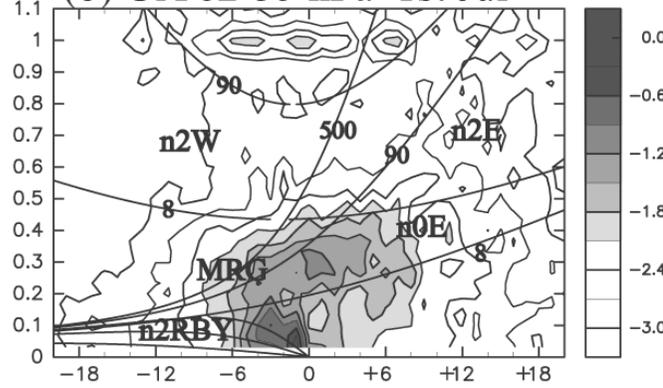
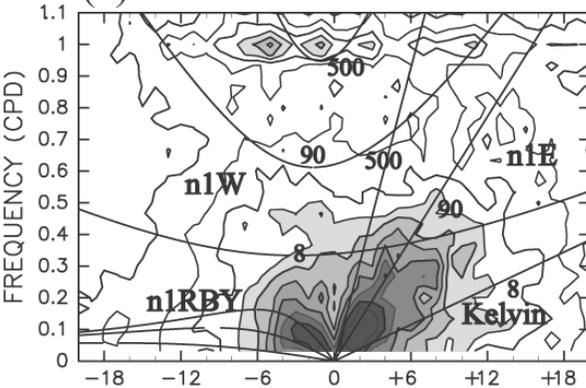
the present model was also one of the
best models for realistically simulating
spectral power at periods of ≤ 6 days.

odd mode: $n = -1, 1$

even mode: $n = 0, 2$

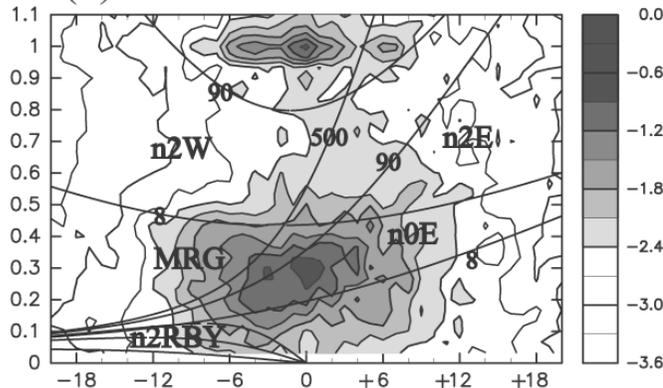
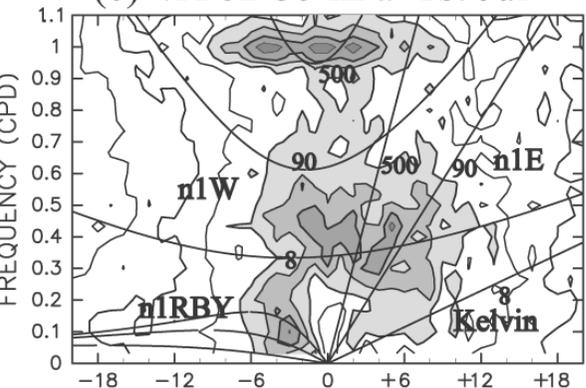
(a) US 82-35 hPa 1st Jul

(b) UA 82-35 hPa 1st Jul



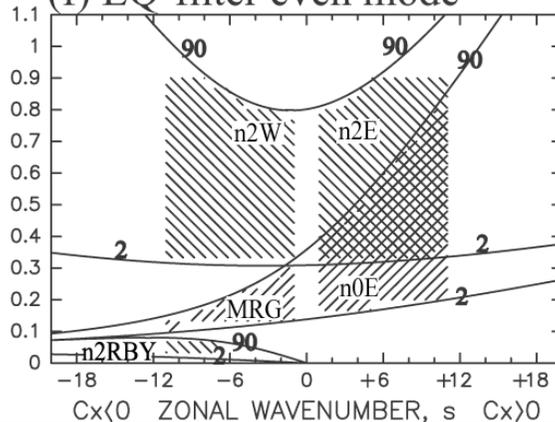
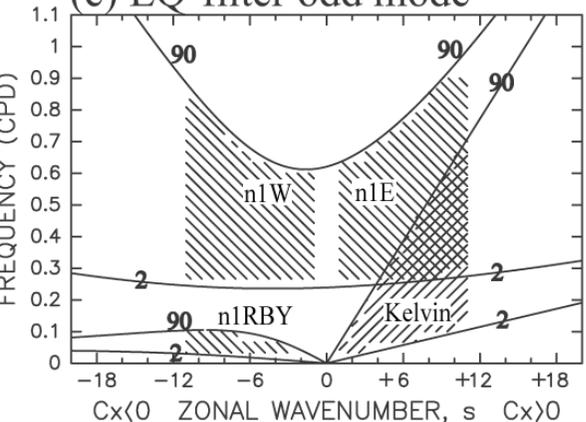
(c) VA 82-35 hPa 1st Jul

(d) VS 82-35 hPa 1st Jul



(e) EQ-filter odd mode

(f) EQ-filter even mode



zonal wavenumber-frequency

U & V spectra

(left) $n = -1, 1$

(right) $n = 0, 2$

(top) zonal wind

(mid) meridional wind

(bottom) EQW filter

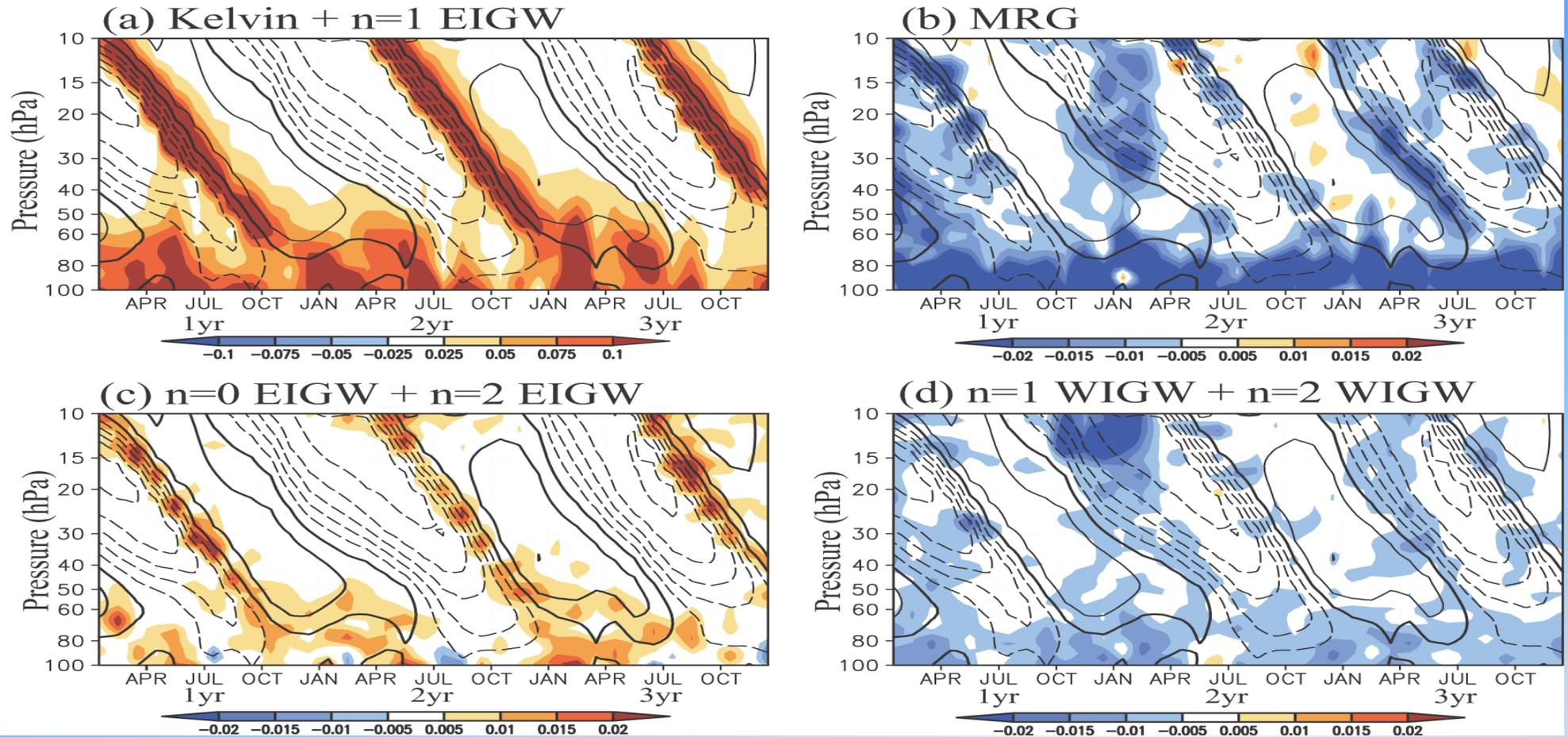
<criteria of EQWs>

- $s = 1 - 11$ ($\lambda_x \geq \sim 3600\text{km}$)
- equivalent depth h : 2-90 (m):
 $\sim 1 \text{ km} \leq \lambda_z \leq \sim 8 \text{ km}$
- minimum periods: 1.1 day
- extracted EQW mode:
 $n = -1 \text{ to } n = 2$

<criteria of internal gravity waves>

- $s \geq 12$ ($\lambda_x \leq \sim 3300 \text{ km}$)

Time-height cross section of EP-flux DIV due to EQWs at 10S-10N



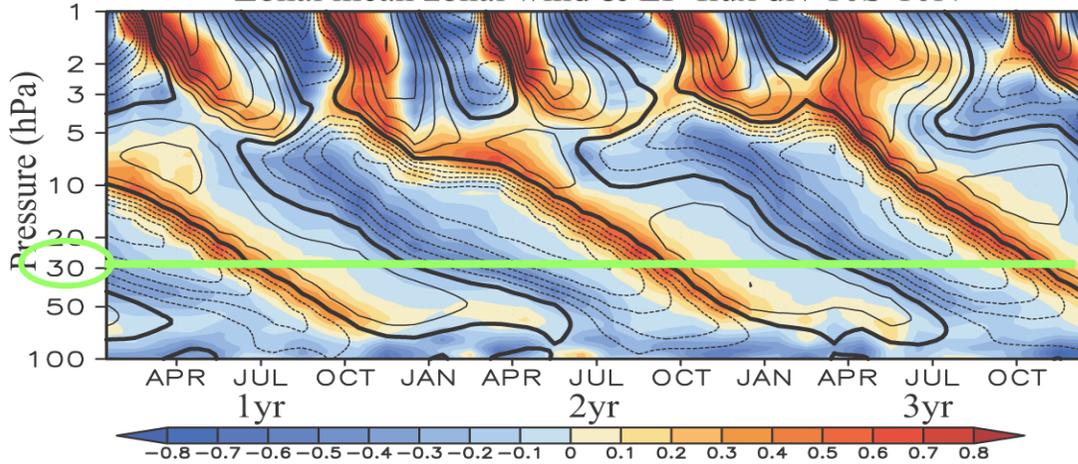
✂ Shading interval of Kelvin + n=1E is 5 times greater than that of other EQWs

Eastward forcing due to odd mode (Kelvin and n=1E waves) \gg even mode (n=0E & n=2E)
July of the 1st year: **odd mode 35%**, **even mode 8 %** contribution of total wave forcing

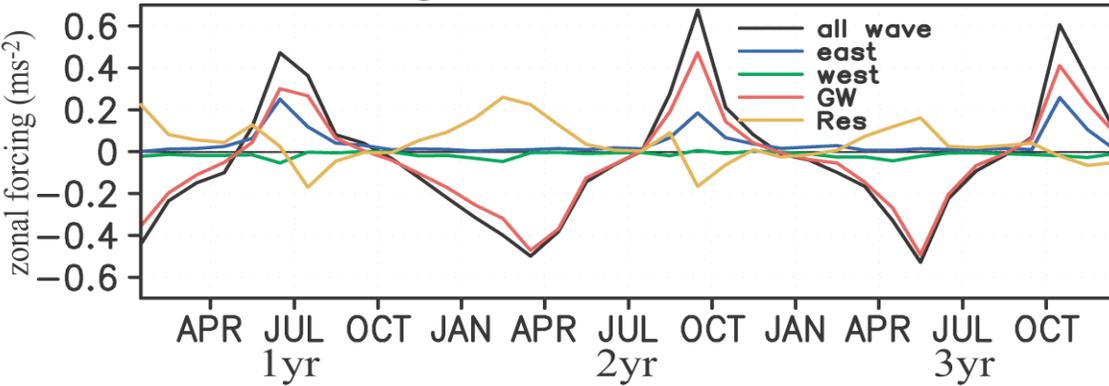
Westward forcing due to MRG waves is stronger than that due to n=1W/n=2W at 20-40hPa

Relative role of EQWs and internal inertia-GWs (10S-10N, 30hPa)

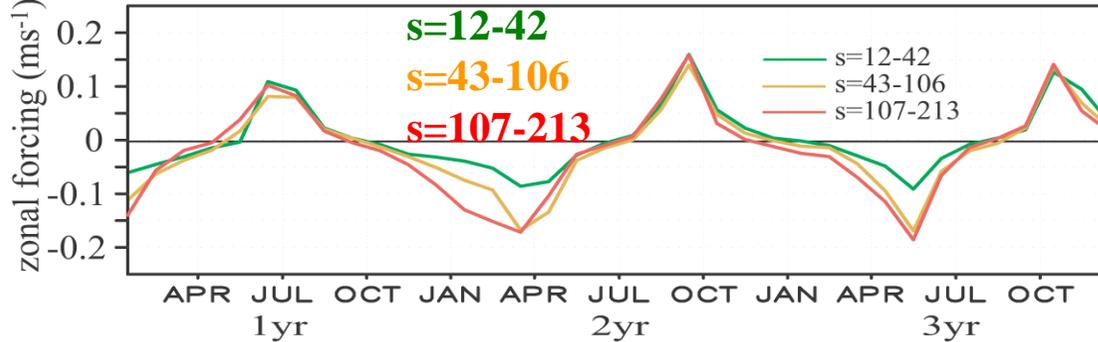
Zonal mean zonal wind & EP-flux div 10S-10N



zonal forcing at 30hPa 10S-10N



EP-flux div with different zonal wavenumbers 30 hPa



<eastward wind shear phase $U_z > 0$ >
 eastward EQWs: $\sim 0.25 \text{ m s}^{-1} \text{ day}^{-1}$
 internal gravity waves: $\sim 0.5 \text{ m s}^{-1} \text{ day}^{-1}$

eastward EQWs: \sim **25-50 %**
 internal GWs: \sim **50-75 %**

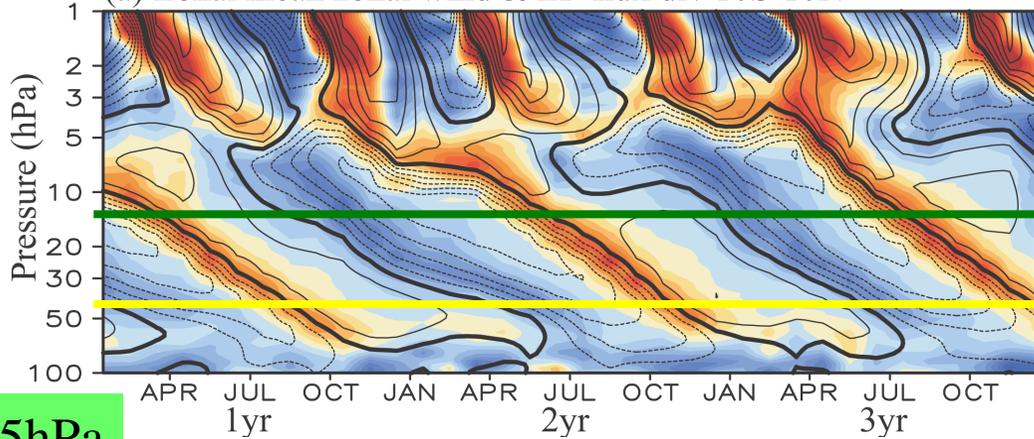
<westward wind shear phase $U_z < 0$ >
 westward EQWs: $\sim -0.05 \text{ m s}^{-1} \text{ day}^{-1}$
 internal gravity waves: $\sim -0.5 \text{ m s}^{-1} \text{ day}^{-1}$

westward EQWs:
 \sim **10%** during **weak westward** wind
 \sim **0 %** during **strong westward** wind

For **westward** wind shear ($U_z < 0$)
 waves with $s \geq 43$ ($\lambda_x \leq \sim 1000 \text{ km}$)

T42 AGCM by Giorgetta et al. (2006)
 resolved wave \rightarrow eastward wind shear
 parameterized wave \rightarrow westward wind shear

(a) Zonal mean zonal wind & EP-flux div 10S-10N



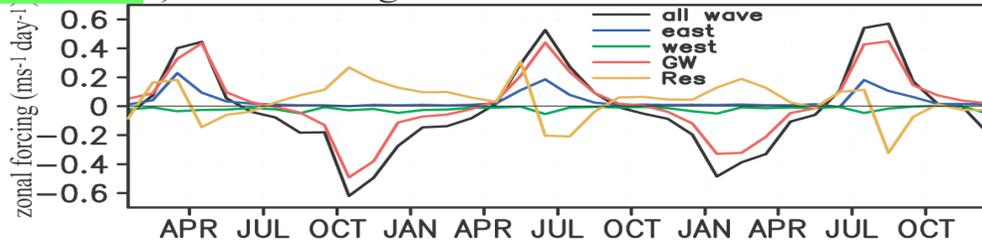
15hPa: extratropical
Rossby wave 10-25%

45hPa: GWs with $s > 106$

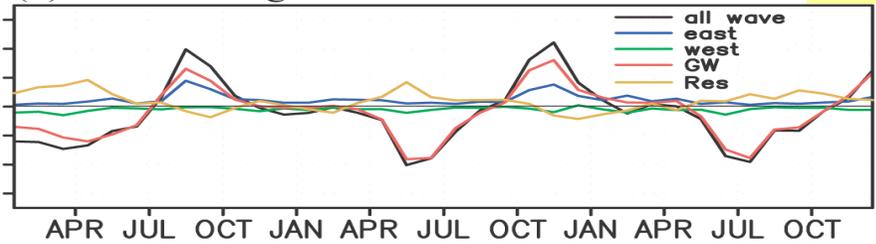
15hPa

45hPa

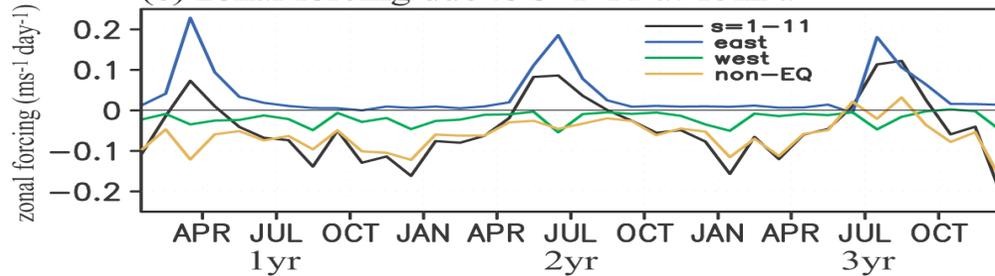
(c) zonal forcing at 15hPa



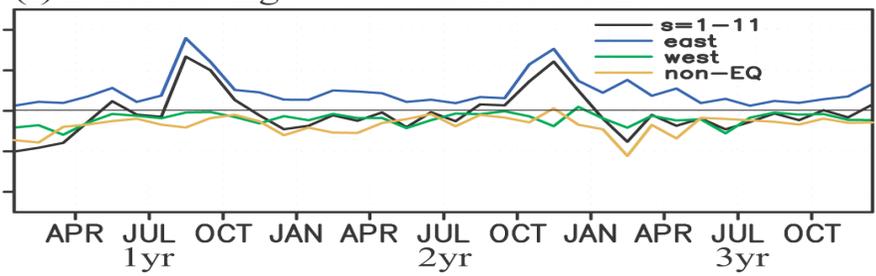
(d) zonal forcing at 45hPa



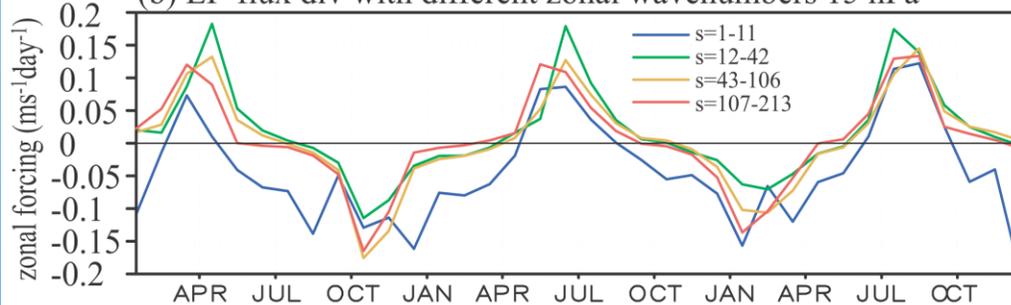
(e) zonal forcing due to $s=1-11$ at 15hPa



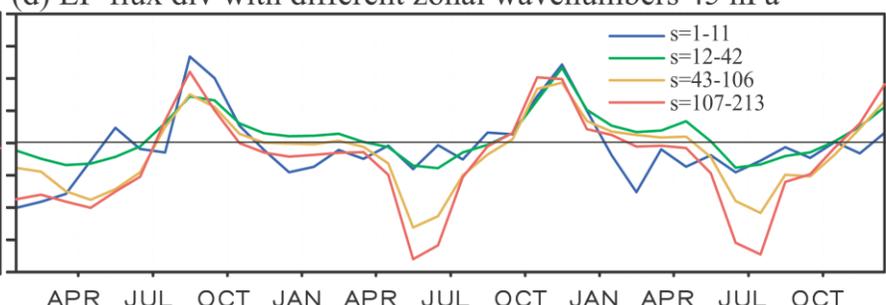
(f) zonal forcing due to $s=1-11$ at 45hPa



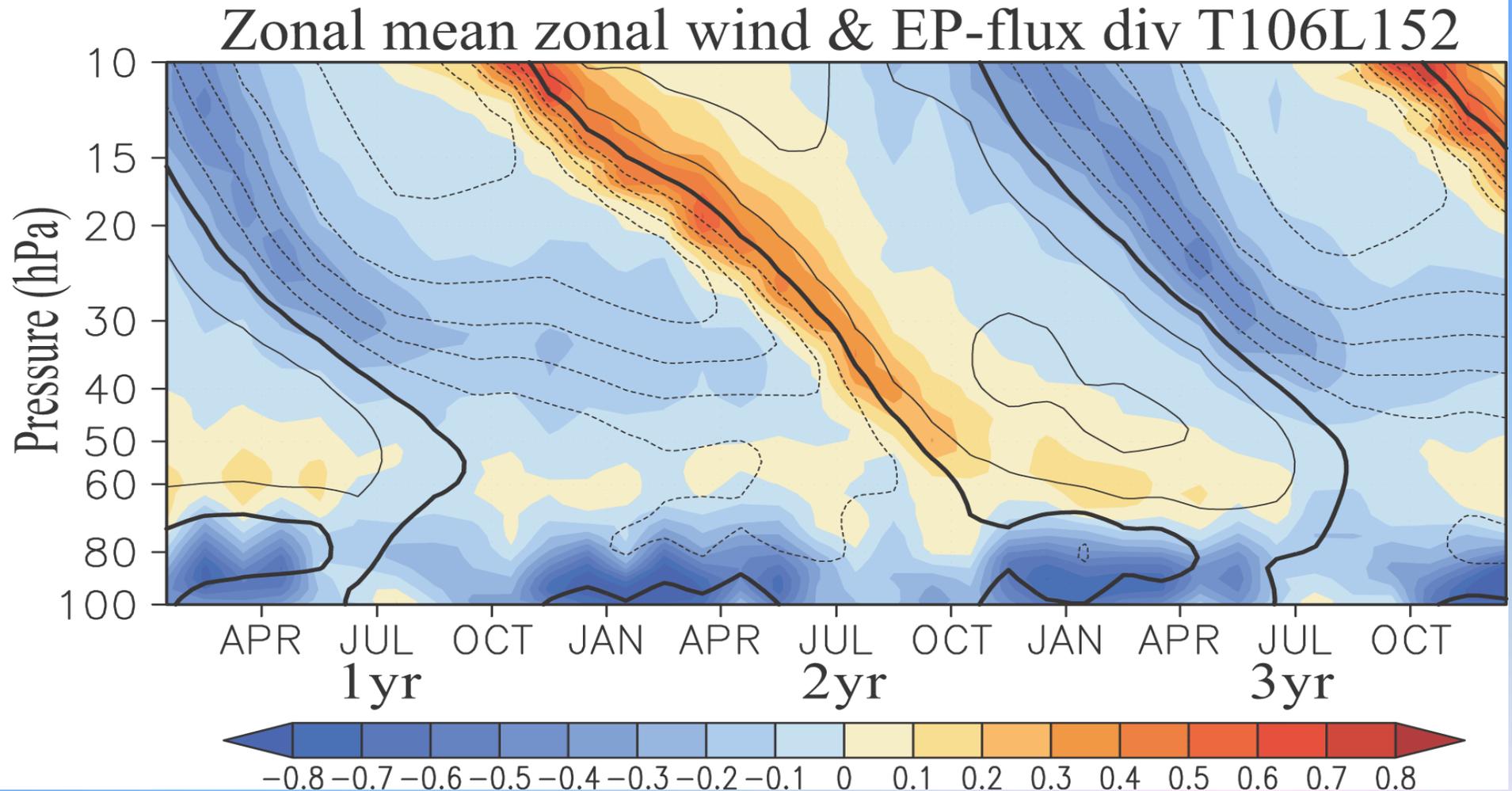
(b) EP-flux div with different zonal wavenumbers 15 hPa



(d) EP-flux div with different zonal wavenumbers 45 hPa



QBO simulated in T106L152



failed to simulate the realistic strictures of the QBO in the lower stratosphere
lowermost level of westward wind phase locates around 45 hPa

T213L256 AGCM: $\Delta h=60\text{km}$, $\Delta z=300\text{m}$, data for 3-year

	EQWs	internal inertia-gravity waves	Extratropical Rossby waves
eastward wind shear	~ 25-50% maximum around 0m/s	~ 50-75% maximum around 0m/s	
westward wind shear	~ 10% during weak westward wind nearly 0% during stronger westward wind	main forcing $\lambda_x \leq \sim 1000\text{km}$ lowermost level of westward wind $\lambda_x \leq \sim 380\text{km}$	~ 10-25% large in the upper level

Analyze 3-year data

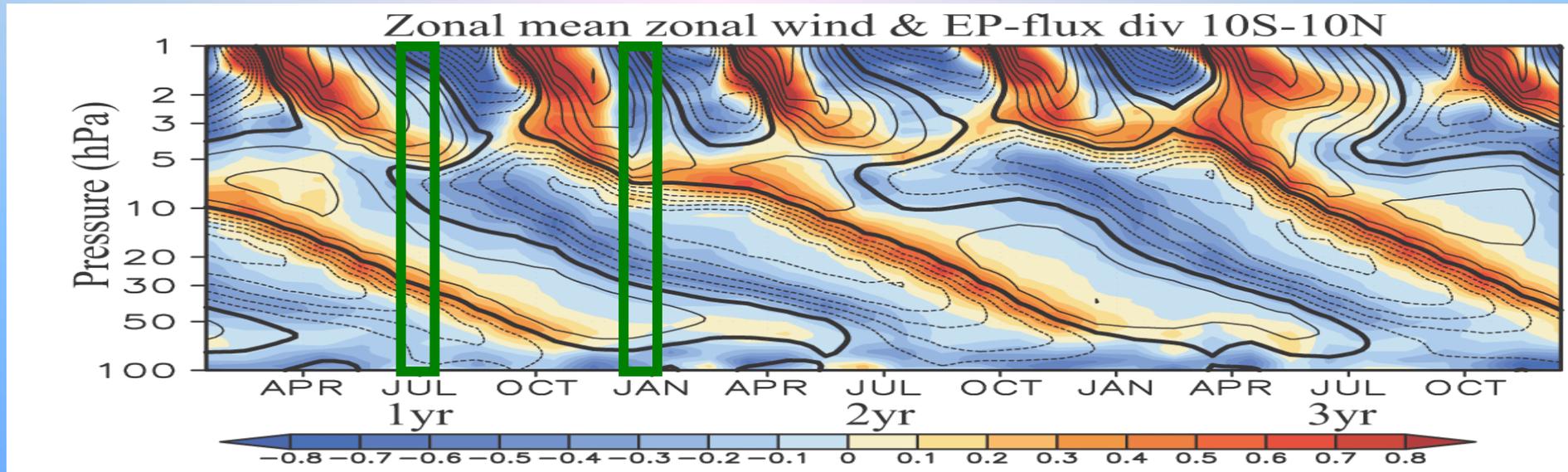
Relative role of EQWs, internal inertia-GWs, extratropical Rossby waves

Roles of waves differ with altitude

3-D distribution of wave forcing

Wave generation and propagation depend greatly on zonal/meridional direction (COSMIC by Alexander et al. 2008a,b; AGCM by Kawatani et al. 2009, JGR)

Model investigations of the 3-D distribution of wave momentum flux and wave forcing should provide useful information for future in situ and satellite observations, as well as for the development of gravity wave parameterization

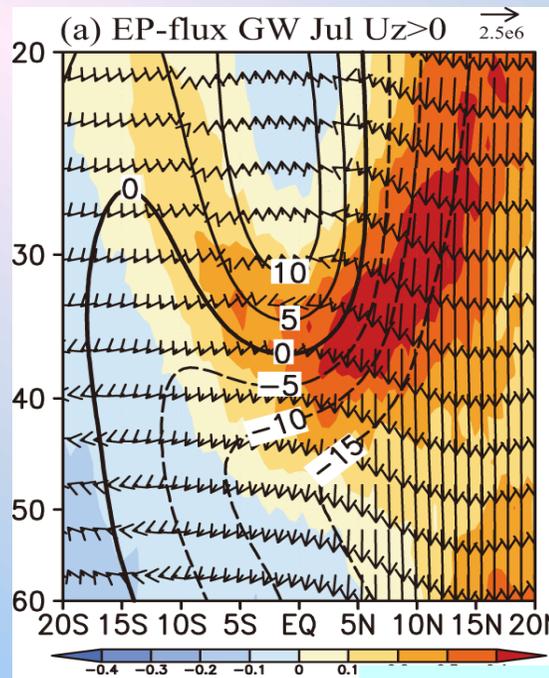


July of the 1st year during eastward wind shear phase ($U_z > 0$)

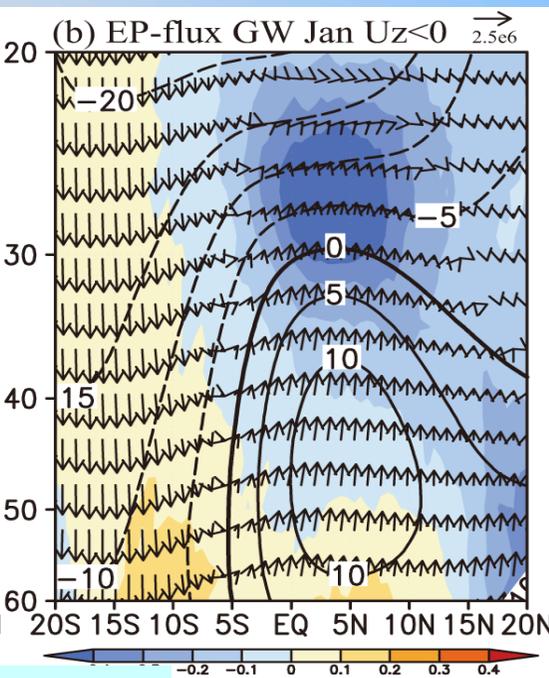
January of the 2nd year during westward wind shear phase ($U_z < 0$)

EP-flux due to internal inertia-gravity waves

$U_z > 0$
Jul

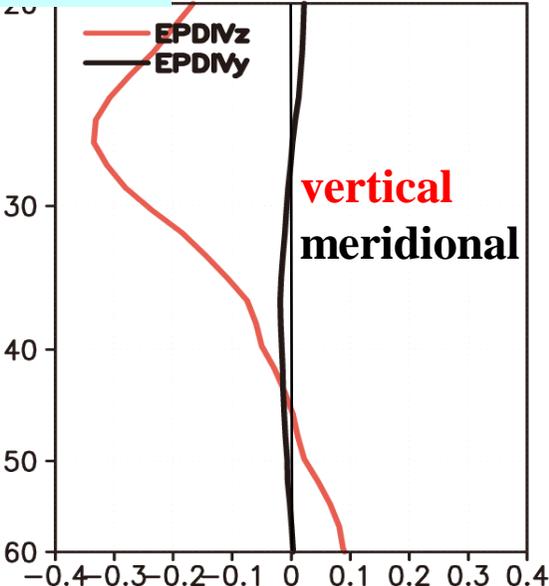
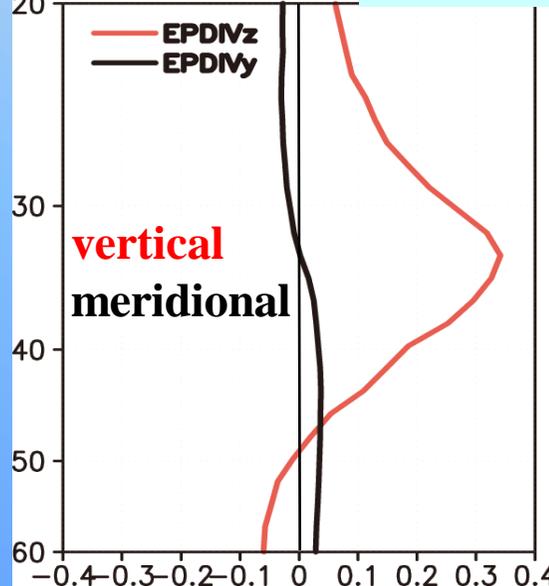


$U_z < 0$
Jan



In both $U_z > 0$ and $U_z < 0$ nearly all EP-flux consist of its **vertical component**

(c) EPDIV y&z 10S Profiles 10S-10N IV y&z 10S-10N Jan

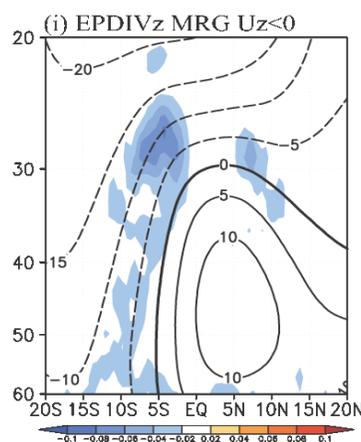
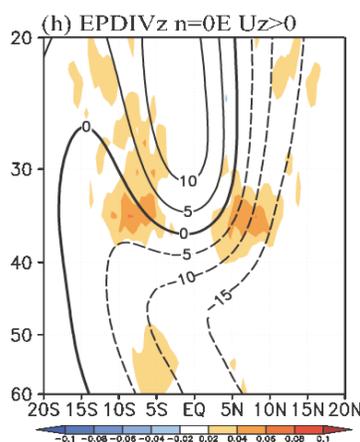
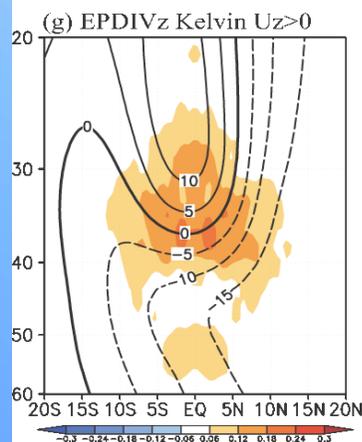
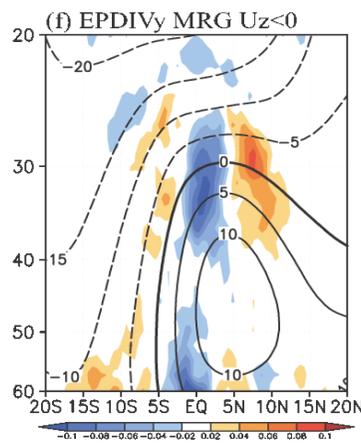
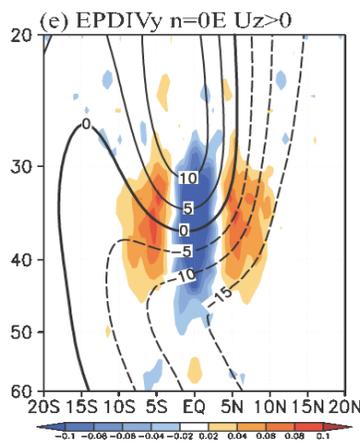
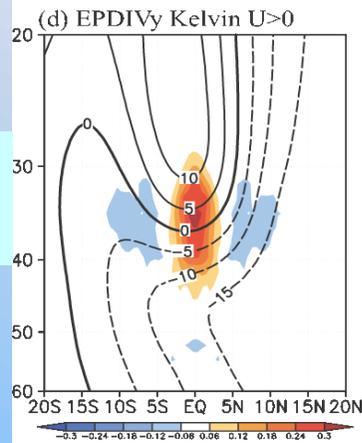
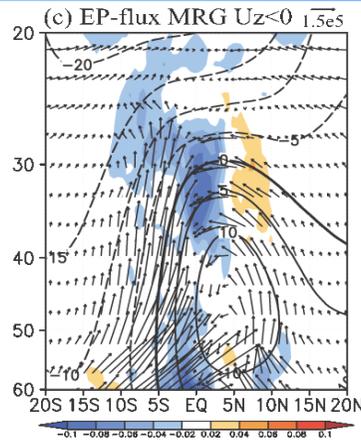
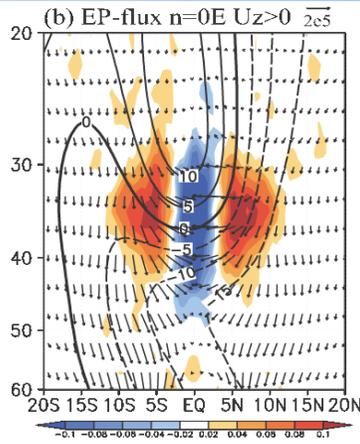
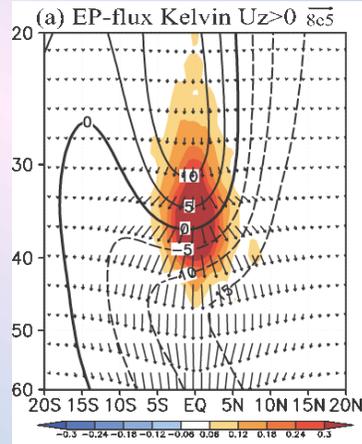


→GWD parameterization including **only vertical wave propagation** is suitable at least for the QBO.

Kelvin: $Uz > 0$

$n=0$ EIGW: $Uz > 0$

MRG: $Uz < 0$



EP-flux
EPDIV

meridional
EPDIV

vertical
EPDIV

<Kelvin>
converge both meridionally
and vertically around $Uz > 0$
eastward forcing is concentrated
on the equator

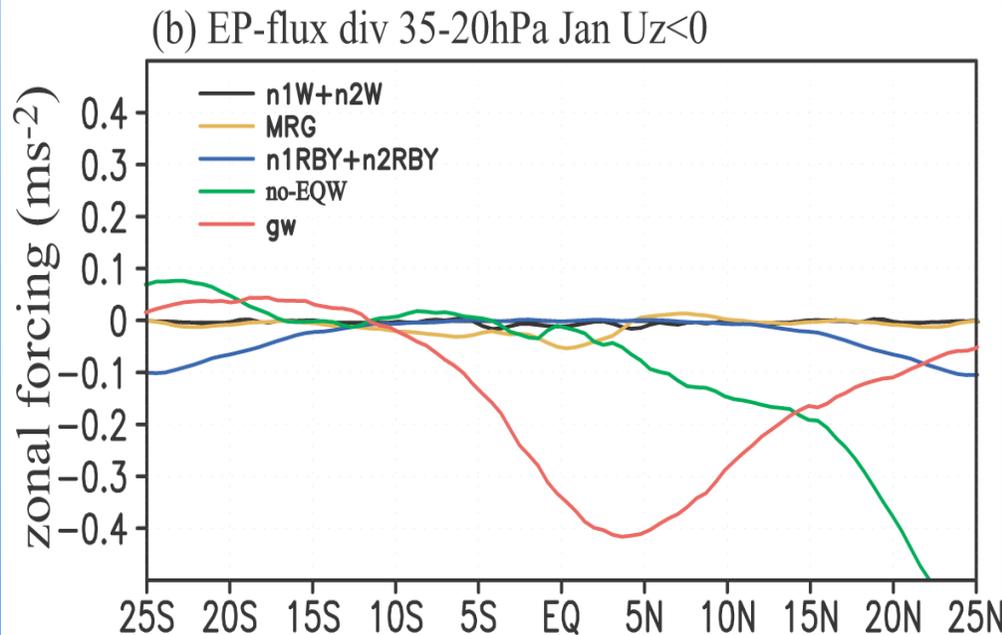
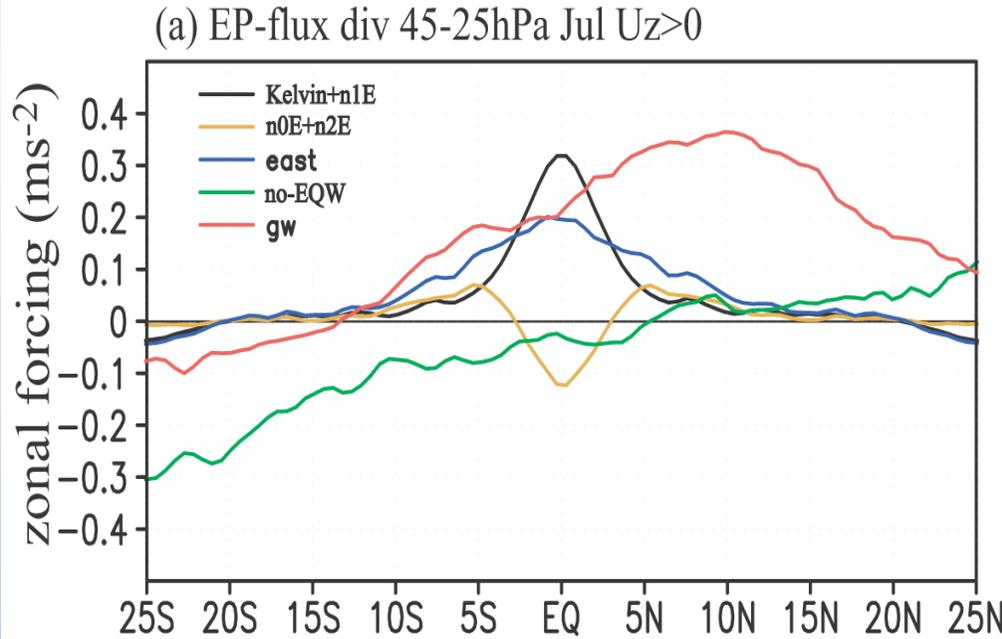
< $n=0$ EIGW>
eastward forcing off the EQ
westward forcing over the EQ

<MRG>
converge both meridionally and
vertically around $Uz < 0$

westward forcing is maximized
around the equator

meridional momentum
transport by EQWs

Latitudinal distribution of the EP-flux divergence



$\langle \text{eastward wind shear } U_z > 0 \rangle$

Kelvin + n1E confined around Eq
 n=0E + n=2E eastward (westward)
 off (over) the equator

Wave forcing due to **internal GWs**
comparable to that due to
eastward EQWs over the Eq
 it prevails off the equator.

Consequently, EQWs contribute to
~38% of total forcing in **10S-10N**

$\langle \text{westward wind shear } U_z < 0 \rangle$

westward EQWs contribute to
~17% over the equator, but the
 contribution is reduced to **~8%**
 in **10S-10N** mean field

extra-tropical Rossby waves
 contribute ~10% in 10S-10N

eastward
 shear

July
 45-25 hPa

westward
 shear

Jan
 35-20 hPa

3-D Wave Activity flux appreciable to inertio-Gravity waves: Miyahara (2006), SOLA, vol.2, 108-111

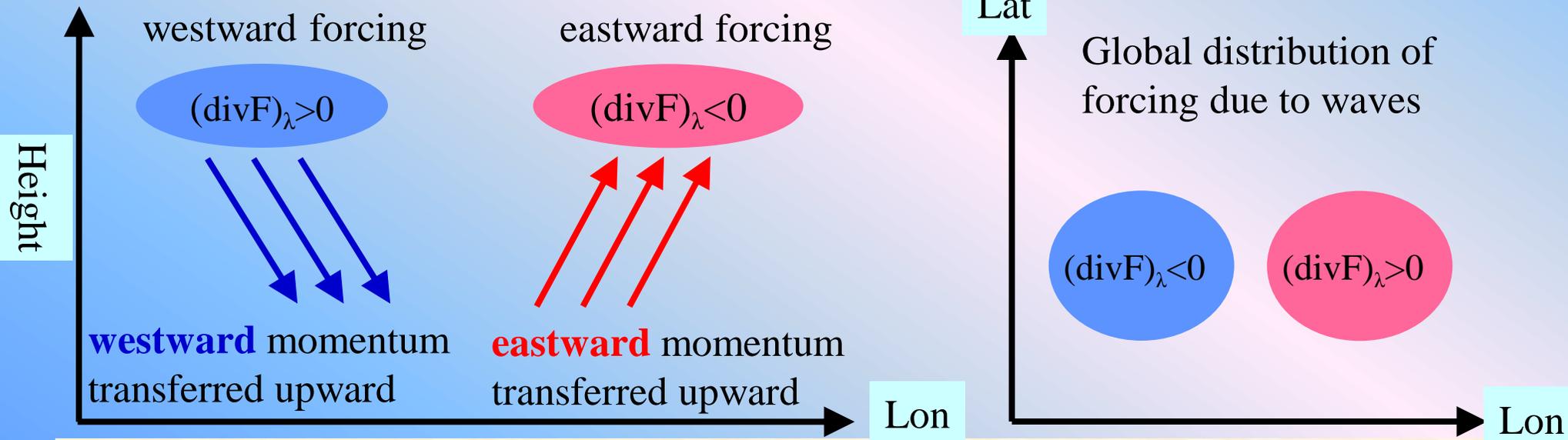
- wave-action density fluxes are relative to the **local time mean** flow

Zonal

$$\frac{D\bar{u}}{Dt} - \frac{\bar{u} \tan \phi}{a} \bar{v} - 2\Omega \sin \phi \bar{v}^* = -\frac{1}{a \cos \phi} \frac{\partial \bar{\Phi}}{\partial \lambda} - (pa \cos \phi)^{-1} (\nabla \cdot F)_\lambda$$

$$F \equiv \begin{bmatrix} \frac{1}{2} \left(\overline{u'^2} - \overline{v'^2} + \frac{\overline{\Phi_z'^2}}{N^2} \right) & \overline{u'v'} & \overline{u'w'} - \frac{2\Omega \sin \phi}{N^2} \overline{v'\Phi_z'} \\ \overline{v'u'} & \frac{1}{2} \left(\overline{v'^2} - \overline{u'^2} + \frac{\overline{\Phi_z'^2}}{N^2} \right) & \overline{v'w'} + \frac{2\Omega \sin \phi}{N^2} \overline{u'\Phi_z'} \\ 0 & 0 & 0 \end{bmatrix} pa \cos \phi$$

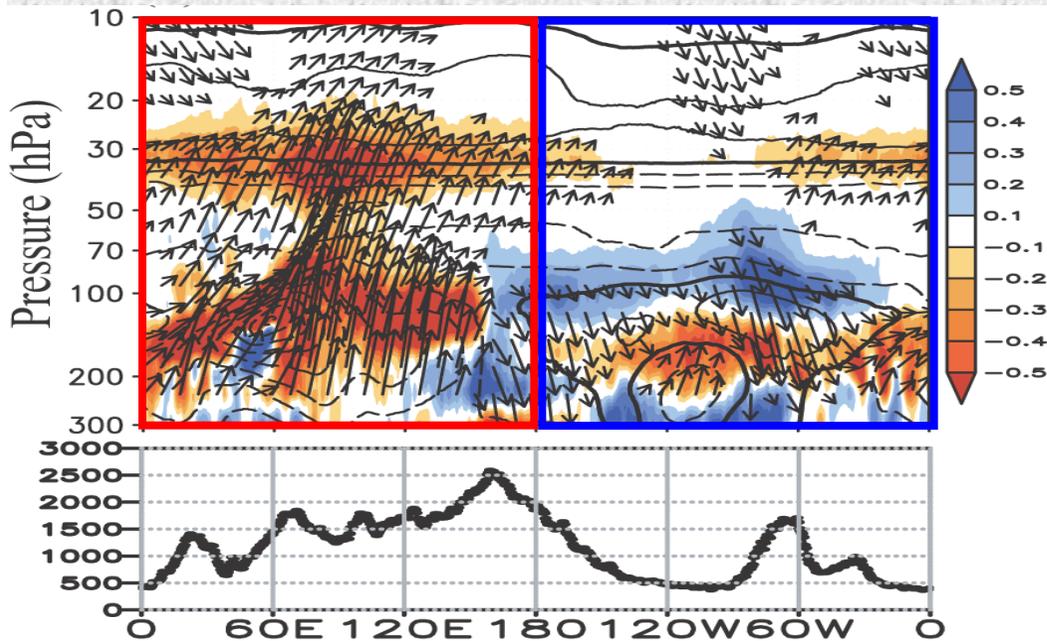
$$F \equiv \begin{bmatrix} \hat{C}_{gx} \frac{E}{\hat{C}_x} & \hat{C}_{gy} \frac{E}{\hat{C}_x} & \hat{C}_{gz} \frac{E}{\hat{C}_x} \\ \hat{C}_{gx} \frac{E}{\hat{C}_y} & \hat{C}_{gy} \frac{E}{\hat{C}_y} & \hat{C}_{gz} \frac{E}{\hat{C}_y} \\ 0 & 0 & 0 \end{bmatrix}$$



Contents of flux tensor F are expressed with intrinsic group velocity and phase velocity

3-D wave flux during $U_z > 0$ in July (10S-10N)

eastward wind shear $U_z > 0$



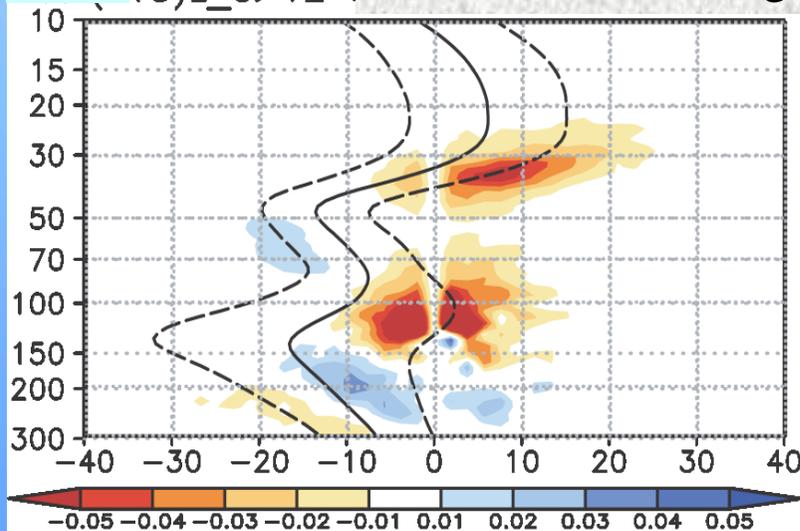
GWs in the EH,
 $-5 \text{ ms}^{-1} < C_x < +20 \text{ ms}^{-1}$
 induce large eastward forcing

GWs in the WH
much smaller contribution
 eastward wind of the Walker circulation
 in the WH prevent eastward GWs
 from entering to the stratosphere

EH

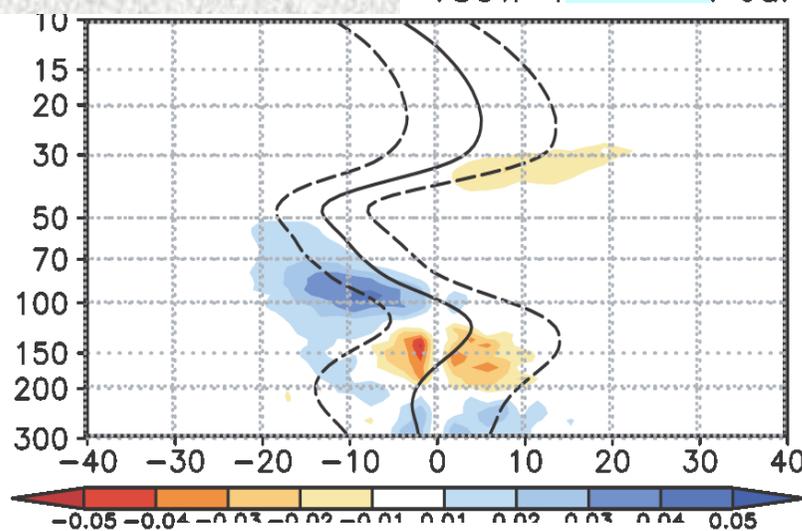
WH

13) $z_s > 12$ (Zonal wave forcing as a function of C_x -180W 1 Jul



westward

eastward



westward

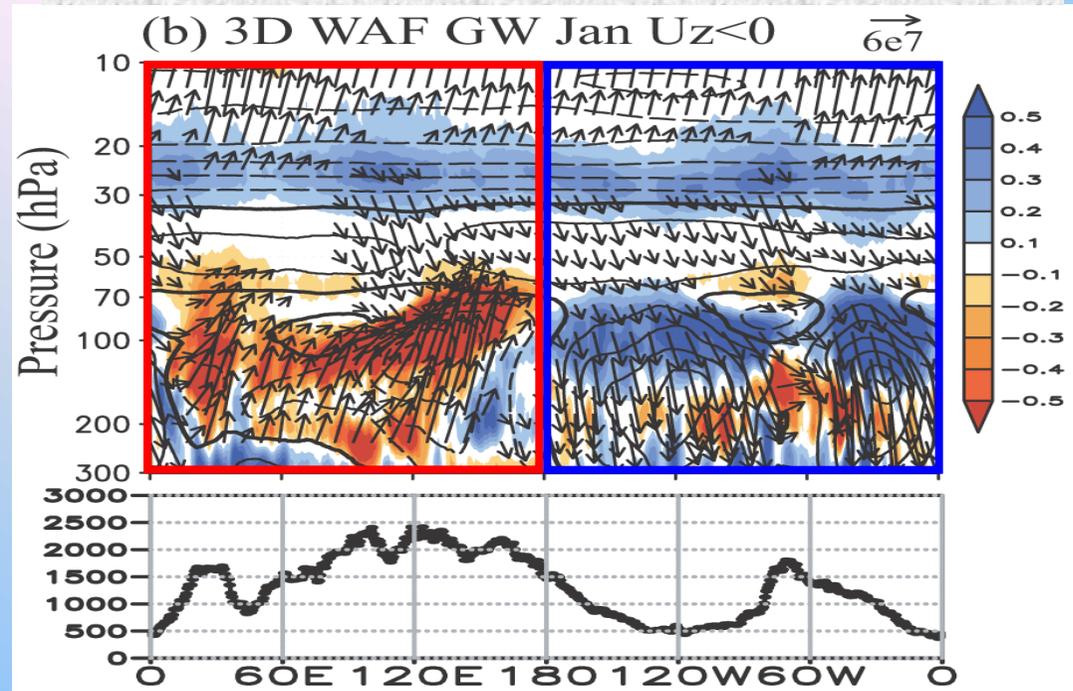
eastward

solid line
 mean zonal wind
 with $s \leq 11$

dashed line
 STD of zonal wind

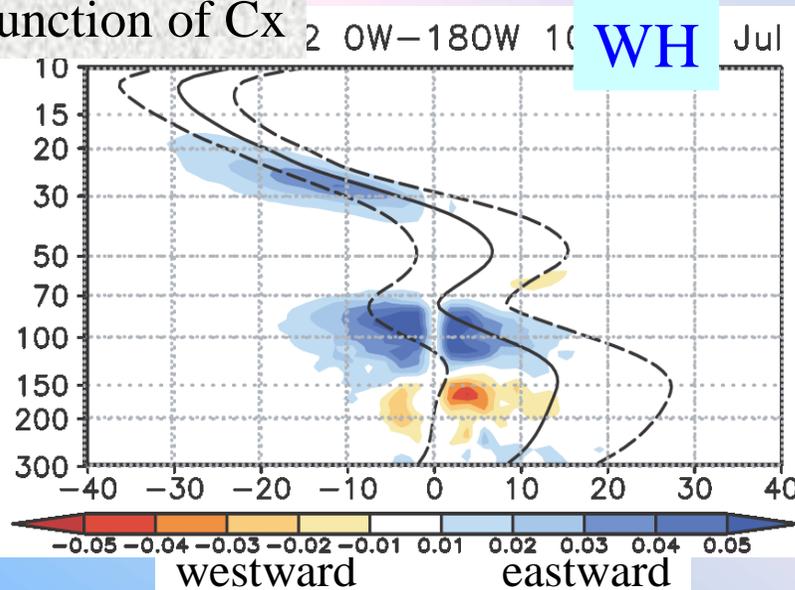
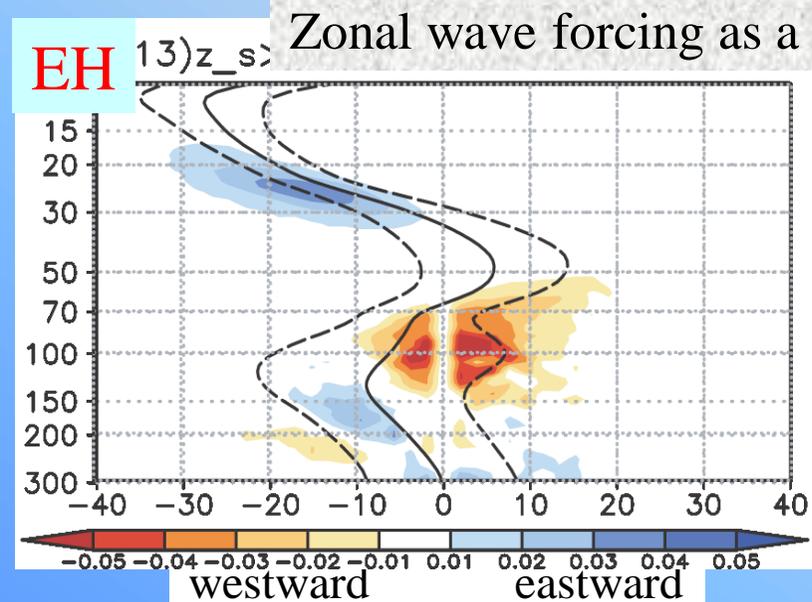
3-D wave flux during $U_z < 0$ in Jan (10S-10N)

westward wind shear $U_z < 0$



GWs $-30 \text{ ms}^{-1} \leq C_x \leq \sim -5 \text{ ms}^{-1}$
small difference between EH & WH
 Larger range of C_x in QBO westward shear zone reduced hemispheric asymmetry
 PRCP in the EH is larger than in the WH

<near top of the Walker circulation>
 EH (WH): eastward (westward) forcing
3-D GWs with small C_x (small λ_z)
dominate around the tropopause



GWs with small C_x around the tropopause
 GWs with small λ_z
 different wave forcing between EH and WH

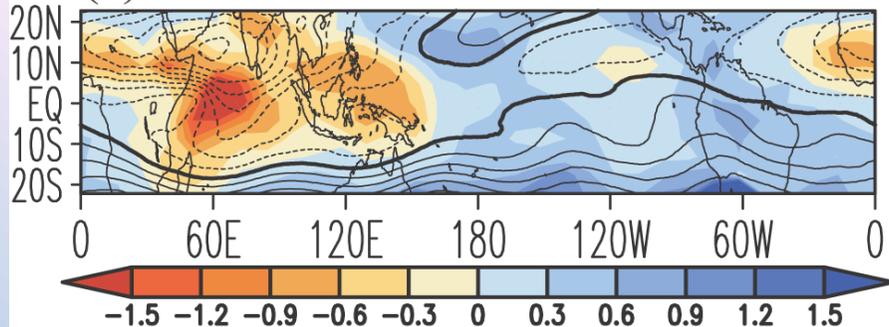
Global distribution of 3-D wave flux divergence associated with internal GWs

Jul, eastward wind shear $U_z > 0$

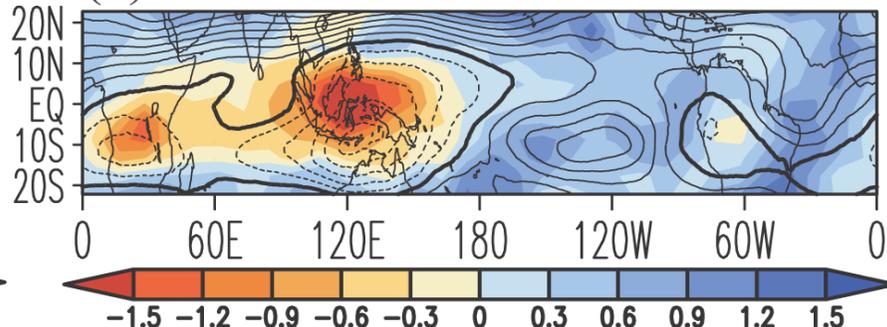
Jan, westward wind shear $U_z < 0$

Top of
Walker
120-80
hPa

(a) GW 3-D flux div Jul 120-80hPa

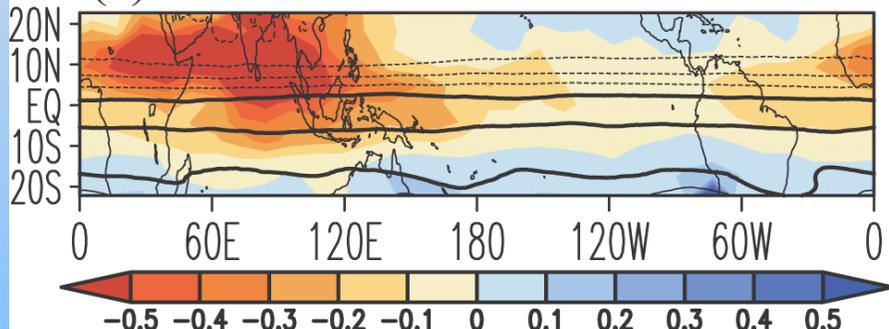


(b) GW 3-D flux div Jan 120-80hPa

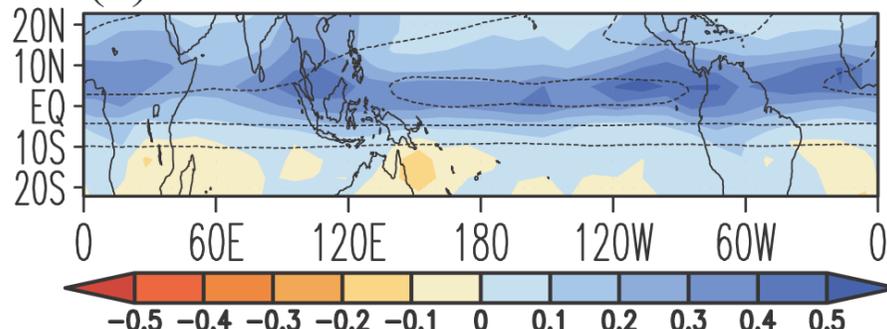


QBO
sheared
~30hPa

(c) GW 3-D flux div Jul 45-25hPa



(d) GW 3-D flux div Jan 35-20hPa



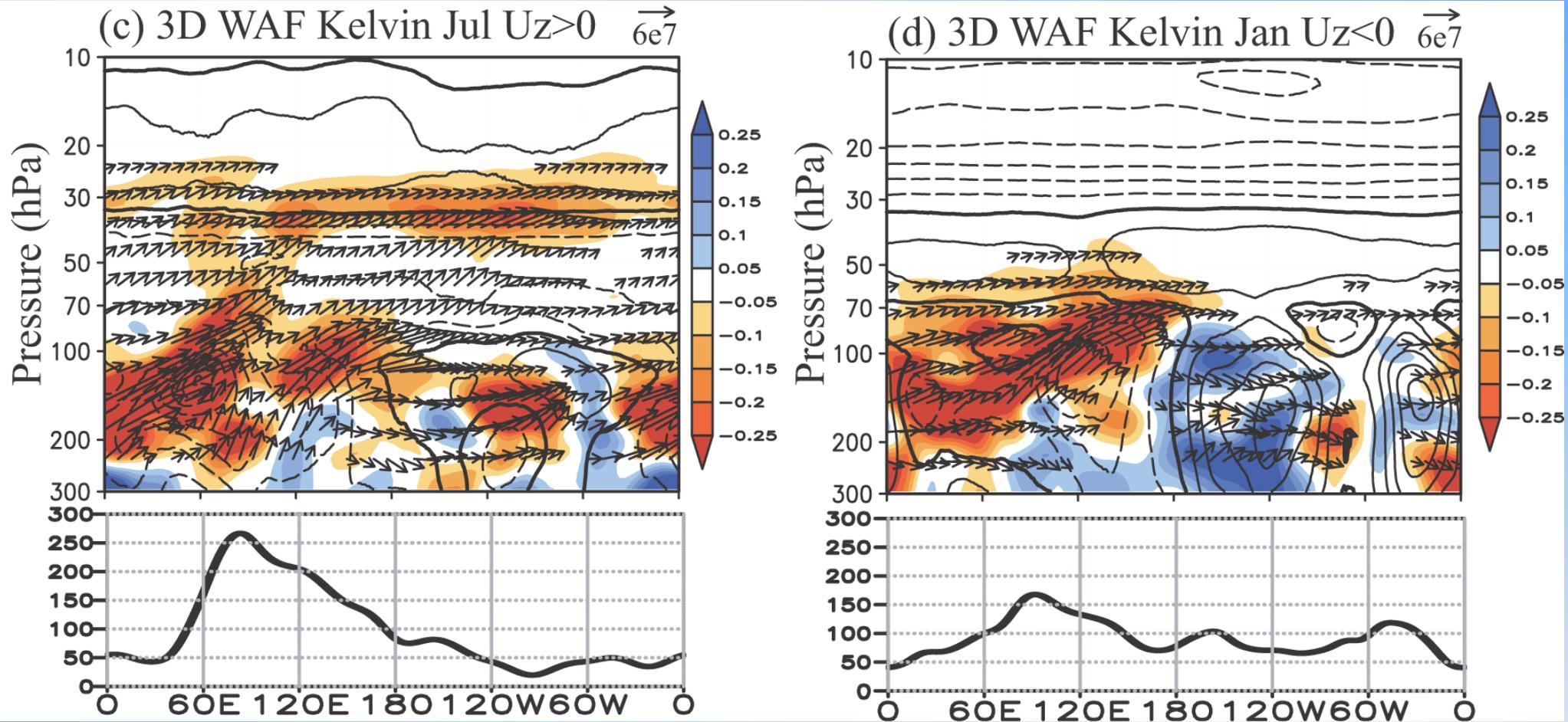
At 120-80 hPa large eastward wave forcing distributes widely in the EH
Zonally inhomogeneous distribution of internal gravity wave forcing is apparent

At 45-25 hPa in Jul, large (very weak) eastward forcing distribute in the EH (WH)
At 35-20 hPa in Jan, westward forcing elongates more zonally over the equatorial region.
(ex. Wave forcing at (100E, 0.2S: EAR) would be stronger than those in other longitudes)

3-D wave flux due to Kelvin waves

eastward wind shear $U_z > 0$

westward wind shear $U_z < 0$



Kelvin wave source is larger in the EH than in the WH
most Kelvin waves generate in the EH propagate into the stratosphere
zonally elongated wave forcing **apart from source region**

Conclusion

T213L256 AGCM: $\Delta h=60\text{km}$, $\Delta z=300\text{m}$, data for 3-year

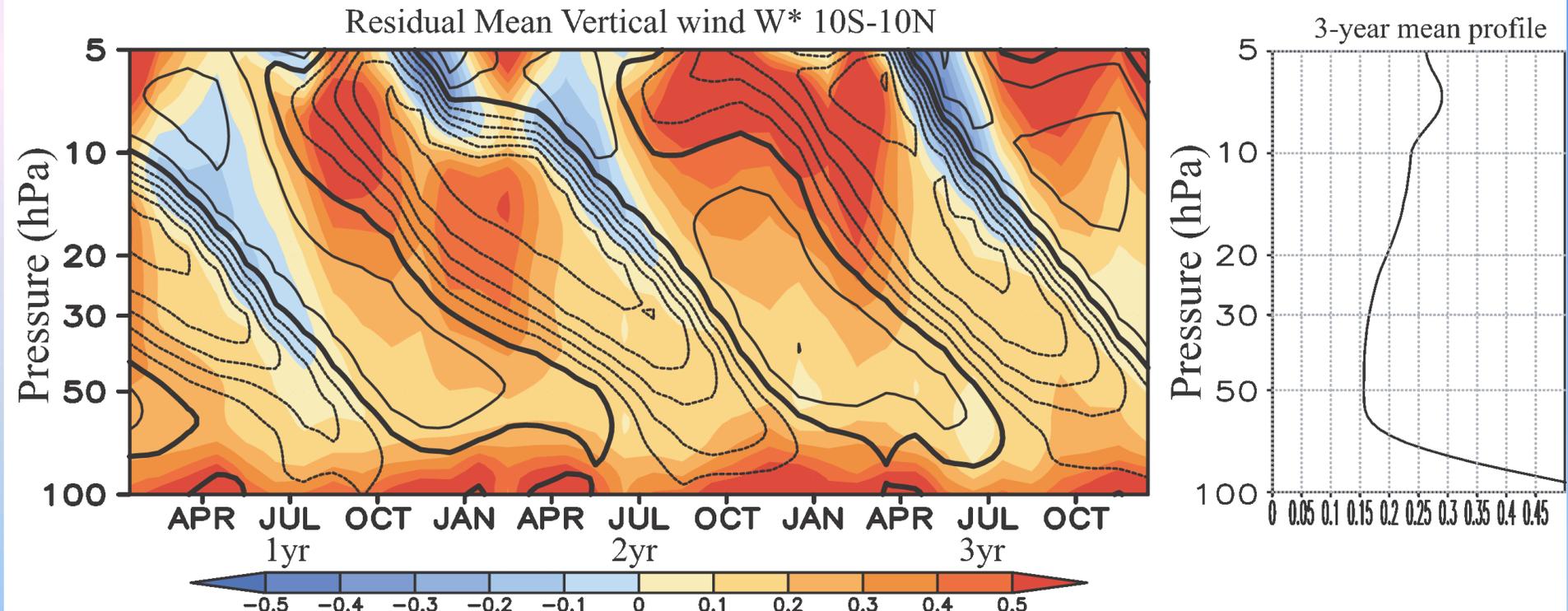
	EQWs	internal inertia-GWs	Extratropical Rossby waves
eastward wind shear	~ 25-50% maximum around 0m/s	~ 50-75% maximum around 0m/s	
westward wind shear	~ 10% during weak westward wind nearly 0% during stronger westward wind	main forcing $\lambda_x \leq \sim 1000\text{km}$ (unresolved by T42)	~ 10-25% large in the upper level

Nearly all EP-flux divergence due to 3-D GWs consists of its vertical components (not shown)
 →GWD parameterization of only vertical wave propagation is suitable for QBO
 Meridional momentum transports by EQWs occurs around vertically sheared zonal winds

The wave forcing to drive the QBO does not show zonally uniform distributions but has large **dependence in the zonal direction**, especially in the eastward wind phase of the QBO (wave momentum flux at (100E, 0S) would have larger than the zonal mean fluxes)

GWs with small $|C_x|$ interact with the top of the Walker circulation, resulting in large eastward (westward) wave forcing in the EH (WH) → short λ_z dominate

Observation (radar, sonde, rocket, satellite) + model (global, regional)



The simulated period of the oscillation is about half that of the QBO in the real atmosphere.

One is underestimation of mean ascent motion in the equatorial lower stratosphere

The other is overestimation of the wave forcing that brings the downward phase of the QBO.

w^* might be half that in the real atmosphere, resulting in the shorter period of simulated QBO.

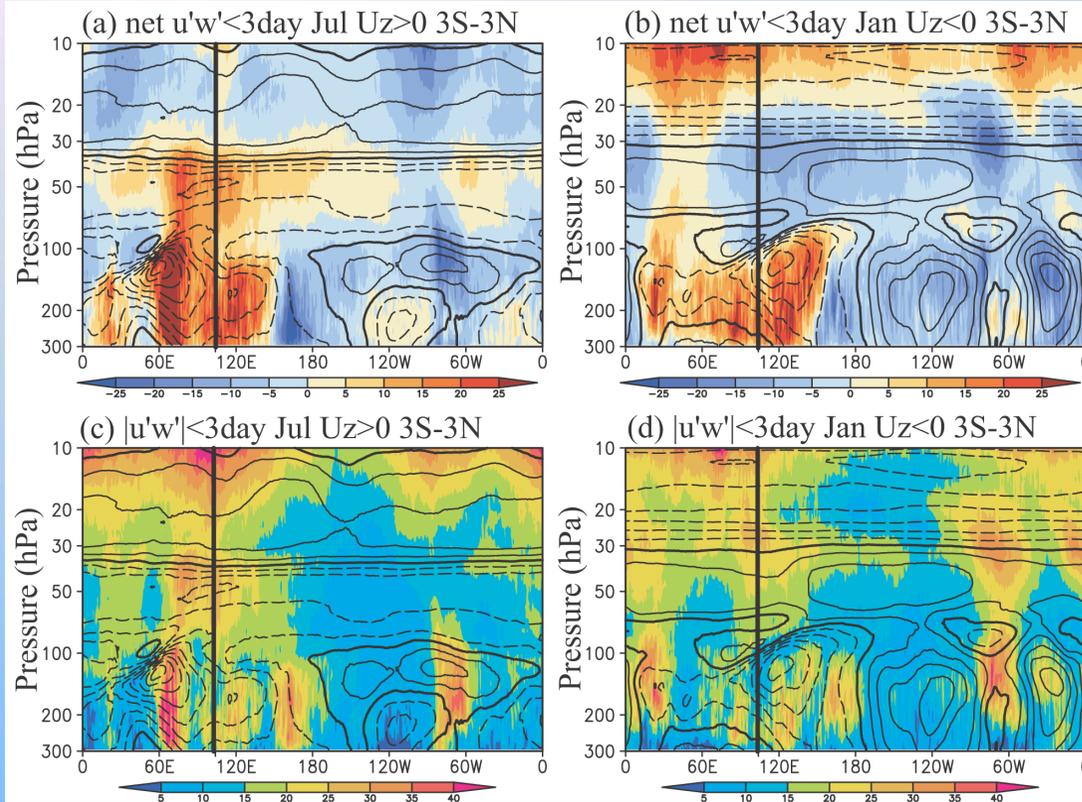
Roughly speaking, we expect that if upwelling in the model were doubled, the rate of eastward shear-zone descent would be reduced by about 0.5 km per month, bringing the total descent rate into better agreement with observations.

The model overestimates the strength of stratospheric westerly in the extratropical winter hemisphere, implying underestimation of wave forcing due to gravity waves and/or Rossby waves in the mid- to high latitudes. Underestimated wave forcing in the mid- to high latitudes would result in weaker in the tropics.

Validation of wave momentum flux

$|u| < 5 \text{ m/s}$

Compared with Sato and Dunkerton (1997)



$U_z > 0$	observation	AGCM
$u'w'$	$0-+4 \times 10^{-3}$	$+10 \times 10^{-3}$
$ u'w' $	$20-60 \times 10^{-3}$	26×10^{-3}

$U_z < 0$	observation	AGCM
$u'w'$	nearly zero	-10×10^{-3}
$ u'w' $	$10-30 \times 10^{-3}$	23×10^{-3}

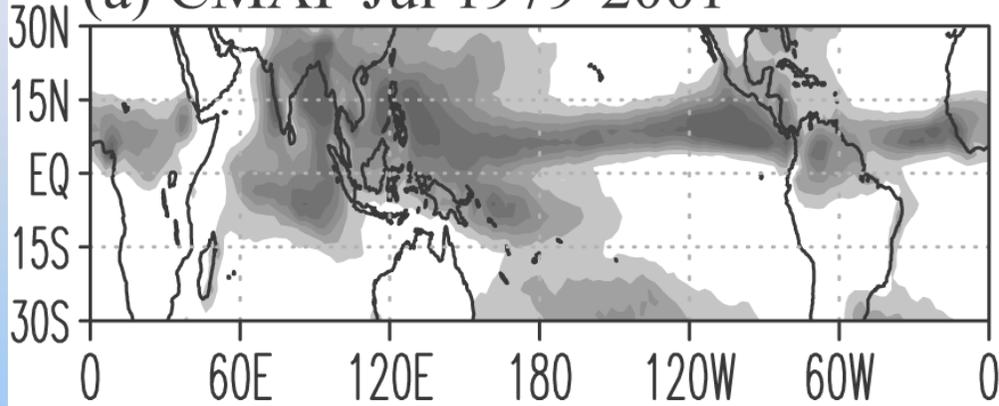
Momentum fluxes with eastward GWs would be simulated reasonably

Momentum fluxes with westward GWs might be a little overestimated

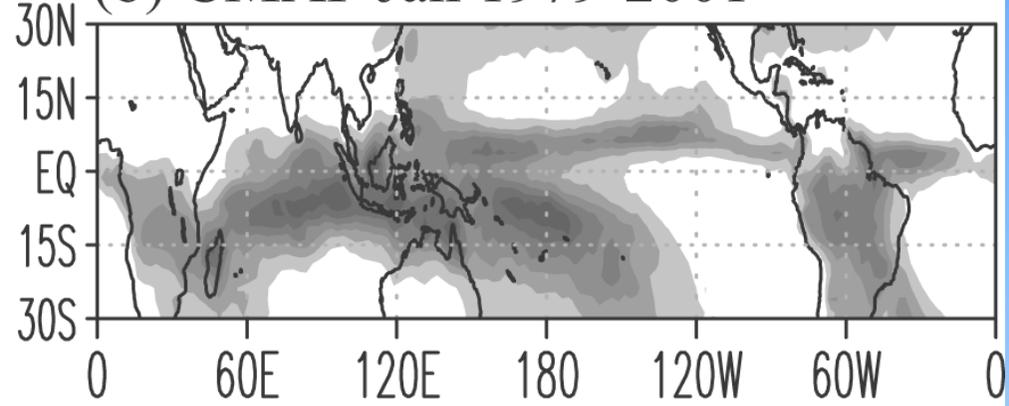
Momentum flux associated with Kelvin waves is simulated realistically (not shown)

Precipitation

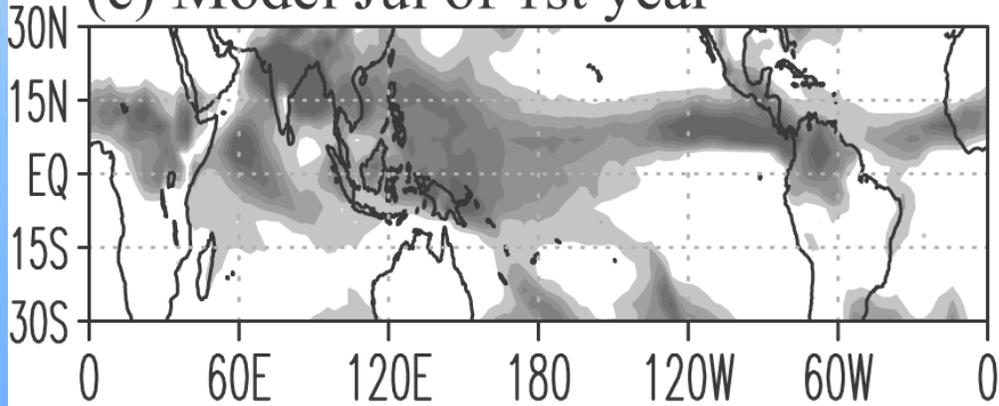
(a) CMAP Jul 1979-2001



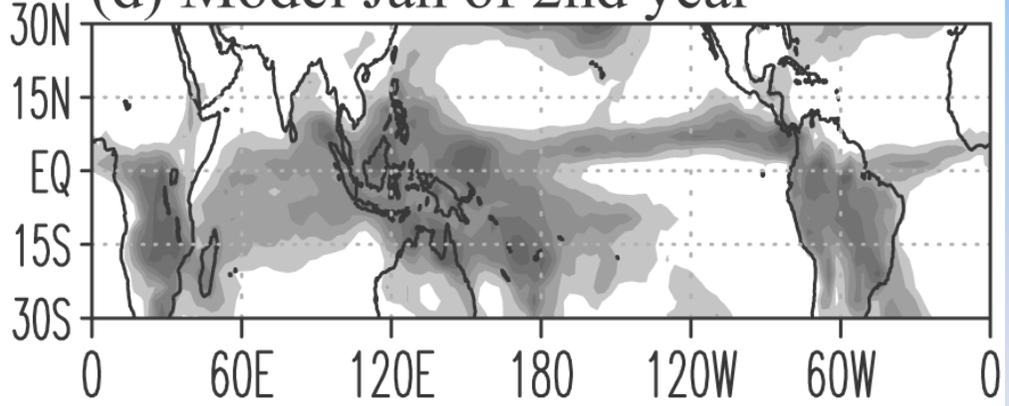
(b) CMAP Jan 1979-2001



(c) Model Jul of 1st year



(d) Model Jan of 2nd year

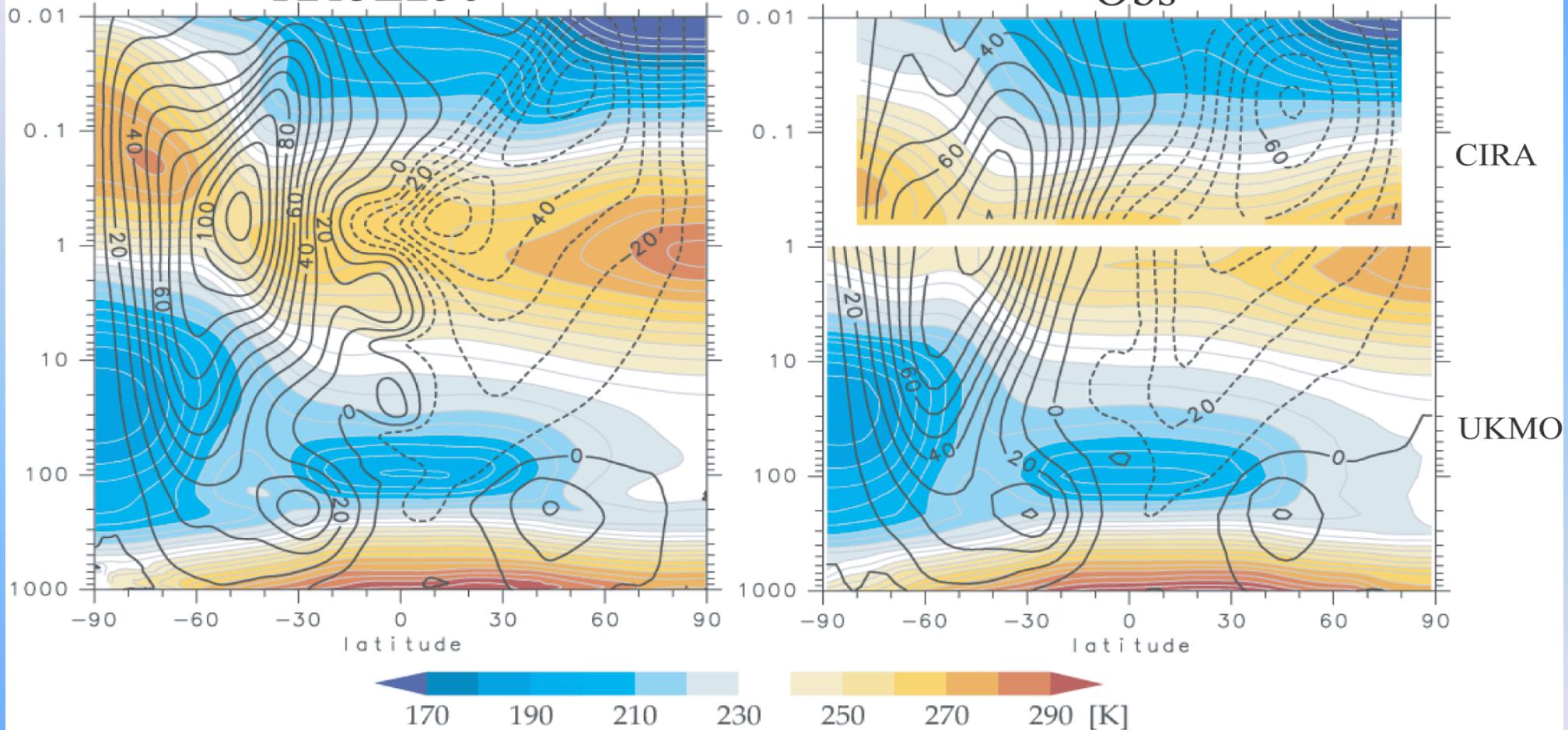


Zonal mean U (contour) & T (color) in July

Zonal Wind (ms^{-1}) and Temperature (K) in July

T213L256

Obs



qualitatively simulates observed structure of U and T

Jet tilts equatorward with height, Stronger westerly, well simulated easterly in mesosphere